

Lecture slides for this course  
have been prepared by Dr. Le Minh Huy,  
EEE, Phenikaa University



# Deep Learning

## Chapter 2 Building Neural Network from Scratch

Dr. Van-Toi NGUYEN  
EEE, Phenikaa University

---

---

---

---

---

---

---

---

1



### Chapter 2: Building Neural Network from Scratch

- 1. Shallow neural network
- 2. Deep neural network
- 3. Building neural network: step-by-step (modulation)
- 4. Regularization
- 5. Dropout
- 6. Batch Normalization
- 7. Optimizers
- 8. Hyper-parameters
- 9. Practice

---

---

---

---

---

---

---

---

2

### Previous Lecture Overview

#### Chapter 1: Course Infor & Programming review - week 1

- 1. Course introduction and grades
- 2. History of Deep learning
- 3. Deep learning applications

#### Chapter 2: Building Neural Network from Scratch - week 2-7

- 1. Shallow neural network - week 2
- 2. Deep neural network - week 3
- 3. Building neural network: step-by-step (modulation) - week 3
- 4. Regularization - week 4
- 5. Dropout - week 4
- 6. Batch Normalization - week 5
- 7. Optimizers - week 6
- 8. Hyper-parameters - week 7
- 9. Practice- week

#### Midterm

#### Chapter 3: Convolutional Neural Network - week 8-10

- 1. Convolutional operator
- 2. History of CNN
- 3. Deep Convolutional Models
- 4. Layers in CNN
- 5. Applications of CNN
- 6. Practice

#### Midterm summary

#### Chapter 4: TensorFlow Library - week 11-13

- 1. Introduction to TensorFlow
- 2. Building a deep neural network with TensorFlow
- 3. Applications
- 4. Practice

#### Chapter 5: Recurrent Neural Network week 14-15

- 1. Unfolding Computational Graphs
- 2. Building a Recurrent Neural Networks
- 3. Long Short-Term Memory
- 4. Vision with Language Processing
- 5. Application of RNN
- 6. Practice

---

---

---

---

---

---

---

---

3

Previous Lecture Overview



45 hours at Classes:  
Theory + Coding practice

90 hours shelf-study at home:  
Theory + Coding practice

---

---

---

---

---

---

---

---

---

---

These slides are provided by Mohitay Le, ICSTLab, Phenikaa Utd.

4

4

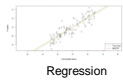
Previous Lecture Overview



**Supervised:** Learning with a **labeled training** set of data  
Example: learn the **classification** of images based on image **labels** (dogs/cats, day time, numbers, etc.)

**Unsupervised:** Discover **patterns in unlabeled data**  
Example: **cluster** similar documents based on text

**Reinforcement learning:** learn to **act** based on **feedback/reward**  
Example: learn to play Go, reward: **win or lose**



Regression



observation



Classification



Clustering

Sources: <http://mlbook.github.io/2013/12/27/machine-learn/>  
<http://www.learningfromhumans.ai/2016-03-26/basics-of-reinforcement-learning-15451a73027/>

These slides are provided by Mohitay Le, ICSTLab, Phenikaa Utd.

5

5

---

---

---

---

---

---

---

---

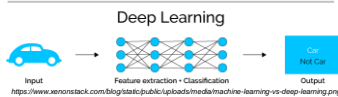
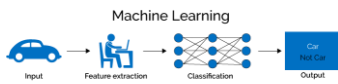
---

---

Previous Lecture Overview



- A sub-field of machine learning for learning **representations** of data.
- Exceptionally effective at **learning patterns**.
- Deep learning algorithms attempt to learn (multiple levels of) representation by using a **hierarchy of multiple layers**
- If you provide the system **tons of information**, it begins to understand it and respond in useful ways.



<https://www.xenonstack.com/blog/stats/public/gp/loads/media/machine-learning-vs-deep-learning.png>

These slides are provided by Mohitay Le, ICSTLab, Phenikaa Utd.

6

6

---

---

---

---

---

---

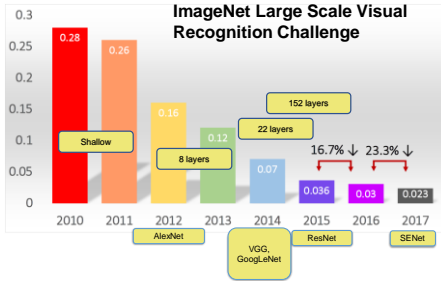
---

---

---

---

Previous Lecture Overview



These slides are provided by Minhuy Le, ICSLab, Phenikaa Utn.

7

7



1. Shallow Neural Network



Basic of Neural Network

- The Perceptron and its Learning Rule (Frank Rosenblatt, 1957)
- Adaptive Linear Neuron and Delta Rule (Widrow & Hoff, 1960)
- Logistic Regression and Gradient Descent

These slides are provided by Minhuy Le, ICSLab, Phenikaa Utn.

8

8

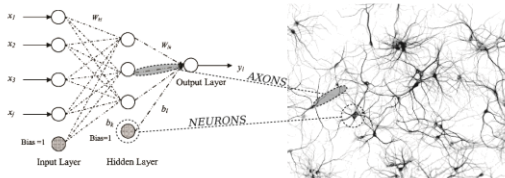


1. Shallow Neural Network



Biologically inspired (akin to the neurons in a brain)

NEURAL NETWORK MAPPING



These slides are provided by Minhuy Le, ICSLab, Phenikaa Utn.

9

9





1. Shallow Neural Network

Frank Rosenblatt's Perceptron (1957)



- To simplify calculations, move  $\theta$  to the origin such that the activation function becomes
- $g(z) = \begin{cases} 1 & \text{if } z \geq 0 \\ -1 & \text{otherwise} \end{cases}$

---

---

---

---

---

---

---

---

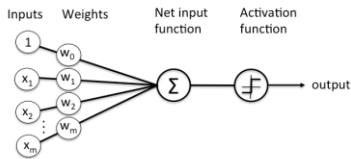
These slides are provided by Minhuy Le, ICSTLab, Phoenikaa Uin.

13

13

1. Shallow Neural Network

Frank Rosenblatt's Perceptron (1957)



Schematic of Rosenblatt's perceptron.

These slides are provided by Minhuy Le, ICSTLab, Phoenikaa Uin.

14

14

---

---

---

---

---

---

---

---

1. Shallow Neural Network

Frank Rosenblatt's Perceptron (1957)



- **Initialize** the weights to 0 or small random numbers.
- For **each training sample**  $x^{(i)}$ :
  - Calculate the **output** value  $y^{(i)} = g(z^{(i)})$
  - **Update** the weights as follows:

$$w_j := w_j + \eta (y^{(i)} - y^{(j)})$$

where  $\eta$  is the learning rate,  $0.0 < \eta < 1$ ,  $y^{(i)}$  is the actual true class label, and  $y^{(j)}$  is the predicted class label.

These slides are provided by Minhuy Le, ICSTLab, Phoenikaa Uin.

15

15

---

---

---

---

---

---

---


---

## 1. Shallow Neural Network

### Frank Rosenblatt's Perceptron (1957)

- Classify the flowers in the **Iris** dataset using the perceptron rule
- Iris dataset from [UCI Machine Learning Repository](https://github.com/mshabimhend/bicbmaster/milestone/classifier/perceptron.py)

More complete version:  
<https://github.com/mshabimhend/bicbmaster/milestone/classifier/perceptron.py>



```
import numpy as np
class Perceptron(object):
    def __init__(self, eta=0.01, epochs=50):
        self.eta = eta
        self.epochs = epochs

    def train(self, X, y):
        self.w_ = np.zeros(1 + X.shape[1])
        self.errors_ = []
        for _ in range(self.epochs):
            errors = 0
            for xi, target in zip(X, y):
                update = self.eta * (target - self.predict(xi))
                self.w_[1:] += update * xi
                self.w_[0] += update
                errors += int(update != 0.0)
            self.errors_.append(errors)
        return self

    def net_input(self, X):
        return np.dot(X, self.w_[1:]) + self.w_[0]

    def predict(self, X):
        return np.where(self.net_input(X) >= 0.0, 1, -1)
```

16

16

## 1. Shallow Neural Network

### Frank Rosenblatt's Perceptron (1957)

Classify 2 flower species: Setosa and Versicolor using sepal length and petal length

- import pandas as pd
- df = pd.read\_csv('https://archive.ics.uci.edu/ml/machine-learning-databases/iris/iris.data', header=None)
- # setosa and versicolor
- y = df.iloc[:, 4].values
- y = np.where(y == 'Iris-setosa', -1, 1)
- # sepal length and petal length
- X = df.iloc[:, 0:2].values


These slides are provided by Mohiboy Le, ICSSLab, Phenikaa Ulu.

17

17

## 1. Shallow Neural Network

### Frank Rosenblatt's Perceptron (1957)



```
%matplotlib inline
import matplotlib.pyplot as plt
from mlxtend.plotting import plot_decision_regions

ppn = Perceptron(epochs=10, eta=0.1)
ppn.train(X, y)
print('Weights: %s' % ppn.w_)
plot_decision_regions(X, y, clf=ppn)
plt.title('Perceptron')

plt.xlabel('sepal length [cm]')
plt.ylabel('petal length [cm]')
plt.show()
plt.plot(range(1, len(ppn.errors_)+1),
         ppn.errors_, marker='o')
plt.xlabel('Iterations')
plt.ylabel('Misclassifications')
plt.show()
```

These slides are provided by Mohiboy Le, ICSSLab, Phenikaa Ulu.

18

18





## 1. Shallow Neural Network

### Adaptive Linear Neurons and the Delta Rule (1960)

$$\begin{aligned}
 \frac{\partial J}{\partial w_j} &= \frac{\partial}{\partial w_j} \frac{1}{2} \sum_i (y^{(i)} - y^{(i)})^2 \\
 &= \frac{1}{2} \sum_i \frac{\partial}{\partial w_j} (y^{(i)} - y^{(i)})^2 \\
 &= \frac{1}{2} \sum_i 2(y^{(i)} - y^{(i)}) \frac{\partial}{\partial w_j} (y^{(i)} - y^{(i)}) \\
 &= \sum_i (y^{(i)} - y^{(i)}) \frac{\partial}{\partial w_j} (y^{(i)} - \sum_j w_j x_j^{(i)}) \\
 &= \sum_i (y^{(i)} - y^{(i)}) (-x_j^{(i)})
 \end{aligned}$$

These slides are provided by Mubhojy Le, ICSTLab, Phenikaa Utn.

25

25

## 1. Shallow Neural Network

### Adaptive Linear Neurons and the Delta Rule (1960)

- A step in gradient descent:
  - $\Delta w_j = -\alpha \frac{\partial J}{\partial w_j} = -\alpha \sum_i (y^{(i)} - y^{(i)}) (-x_j^{(i)}) = \alpha \sum_i (y^{(i)} - y^{(i)}) x_j^{(i)}$
- Update weight vector:
  - $\mathbf{w} := \mathbf{w} + \Delta \mathbf{w}$
- Differences with the perceptron rule
  - The output  $y^{(i)}$  is a **real number**, not a class label as in perceptron learning rule.
  - Weight update is based on “**all samples in the training set**” (Batch GD)

These slides are provided by Mubhojy Le, ICSTLab, Phenikaa Utn.

26

26

## 1. Shallow Neural Network

### Adaptive Linear Neurons and the Delta Rule (1960)

```

import numpy as np

class AdalineGD(object):
    def __init__(self, alpha=0.01, epochs=50):
        self.alpha = alpha
        self.epochs = epochs
    def train(self, X, y):
        self.w_ = np.zeros(1 + X.shape[1])
        self.cost_ = []
        for i in range(self.epochs):
            output = self.net_input(X)
            errors = (y - output)
            self.w_[1:] += self.alpha * X.T.dot(errors)
            self.w_[0] += self.alpha * errors.sum()
            cost = (errors**2).sum() / 2.0
            self.cost_.append(cost)
        return self

    def net_input(self, X):
        return np.dot(X, self.w_[1:]) + self.w_[0]
    def activation(self, X):
        return self.net_input(X)
    def predict(self, X):
        return np.where(self.activation(X) >= 0.0, 1, -1)

```

These slides are provided by Mubhojy Le, ICSTLab, Phenikaa Utn.

27

27



1. Shallow Neural Network

Adaptive Linear Neurons and the Delta Rule (1960)



```
# standardize features
X_std = np.copy(X)
X_std[:,0] = (X[:,0] - X[:,0].mean()) / X[:,0].std()
X_std[:,1] = (X[:,1] - X[:,1].mean()) / X[:,1].std()
```

---

---

---

---

---

---

---

---

---

---

These slides are provided by Mohibuy Le, ICSTLab, PheNiKaa Uth.

31

31

1. Shallow Neural Network

Adaptive Linear Neurons and the Delta Rule (1960)



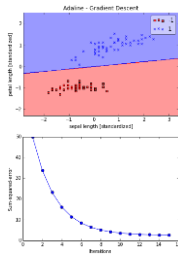
```
%matplotlib inline
import matplotlib.pyplot as plt
from sklearn.preprocessing import StandardScaler

ada = AdaLinsGD(epochs=15, eta=0.01)

ada.train(X_std, y)

plt.figure(figsize=(10, 10))
plt.subplot(2, 1, 1)
plt.title('Adaline - Gradient Descent')
plt.xlabel('sepal length (standardized)')
plt.ylabel('petal length (standardized)')
plt.show()

plt.subplot(2, 1, 2)
plt.title('Adaline - Gradient Descent')
plt.xlabel('Iteration')
plt.ylabel('Sum-squared error')
plt.show()
```



These slides are provided by Mohibuy Le, ICSTLab, PheNiKaa Uth.

32

32

---

---

---

---

---

---

---

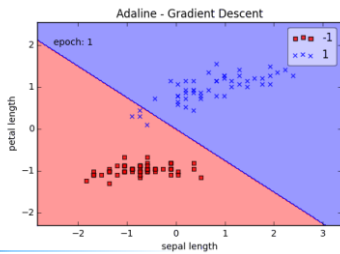
---

---

---

1. Shallow Neural Network

Adaptive Linear Neurons and the Delta Rule (1960)



These slides are provided by Mohibuy Le, ICSTLab, PheNiKaa Uth.

33

33

---

---

---

---

---

---

---

---

---

---

## 1. Shallow Neural Network

### Adaptive Linear Neurons and the Delta Rule (1960)



```
import numpy as np

class AdalineSGD(object):
    def __init__(self, alpha=0.01, epochs=50):
        self.alpha = alpha
        self.epochs = epochs
    def train(self, X, y, reinitialize_weights=True):
        if reinitialize_weights:
            self.w_ = np.zeros(1 + X.shape[1])
            self.cost_ = []
        for i in range(self.epochs):
            for xi, target in zip(X, y):
                output = self.net_input(xi)
                error = (target - output)
                self.w_[1:] += self.alpha * xi.dot(error)
                self.w_[0] += self.alpha * error
            cost = ((y - self.activation(X))**2).sum() / 2.0
            self.cost_.append(cost)
        return self

    def net_input(self, X):
        return np.dot(X, self.w_[1:]) + self.w_[0]

    def activation(self, X):
        return self.net_input(X)

    def predict(self, X):
        return np.where(self.activation(X) >= 0.0, 1, -1)
```

These slides are provided by Mohiboy Lu, ICSLab, Phenikaa Uin.

34

34

## 1. Shallow Neural Network

### Adaptive Linear Neurons and the Delta Rule (1960)



- **Batch Gradient Descent (BGD)**
  - Cost function is minimized based on the complete training dataset (all samples)
- **Stochastic Gradient Descent (SGD)**
  - Weights are incrementally updated after each individual training sample
  - Converges faster than BGD since weights are updated immediately after each training sample
  - Computationally more efficient, especially for large datasets
- **Mini-batch Gradient Descent (MGD)**
  - Compromise between BGD and SGD, dataset is divided into mini-batches
  - Smoother convergence than SGD

These slides are provided by Mohiboy Lu, ICSLab, Phenikaa Uin.

35

35

## 1. Shallow Neural Network

### Adaptive Linear Neurons and the Delta Rule (1960)

### Adaline with SGD



```
import numpy as np

class AdalineSGD(object):
    def __init__(self, alpha=0.01, epochs=50):
        self.alpha = alpha
        self.epochs = epochs
    def train(self, X, y, reinitialize_weights=True):
        if reinitialize_weights:
            self.w_ = np.zeros(1 + X.shape[1])
            self.cost_ = []
        for i in range(self.epochs):
            for xi, target in zip(X, y):
                output = self.net_input(xi)
                error = (target - output)
                self.w_[1:] += self.alpha * xi.dot(error)
                self.w_[0] += self.alpha * error
            cost = ((y - self.activation(X))**2).sum() / 2.0
            self.cost_.append(cost)
        return self

    def net_input(self, X):
        return np.dot(X, self.w_[1:]) + self.w_[0]

    def activation(self, X):
        return self.net_input(X)

    def predict(self, X):
        return np.where(self.activation(X) >= 0.0, 1, -1)
```

These slides are provided by Mohiboy Lu, ICSLab, Phenikaa Uin.

36

36







1. Shallow Neural Network

Logistic Regression

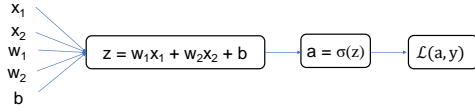
Computation Graph



$$z = w^T x + b$$

$$\hat{y} = a = \sigma(z)$$

$$\mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$$




---

---

---

---

---

---

---

---

---

---

These slides are provided by Minhhoai Le, ICSTLab, Phoenicia Ltd.

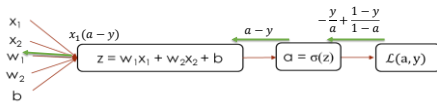
46

46

1. Shallow Neural Network

Logistic Regression

Computation Graph



$$\begin{aligned} \cdot \frac{\delta L(a, y)}{\delta a} &= \left( -\frac{y}{a} + \frac{1-y}{1-a} \right) \\ \cdot \frac{\delta L(a, y)}{\delta z} &= \frac{\delta L(a, y)}{\delta a} \frac{\delta a}{\delta z} = \left( -\frac{y}{a} + \frac{1-y}{1-a} \right) (a(1-a)) = a - y \\ \cdot \frac{\delta L(a, y)}{\delta w_1} &= \frac{\delta L(a, y)}{\delta a} \frac{\delta a}{\delta z} \frac{\delta z}{\delta w_1} = \left( -\frac{y}{a} + \frac{1-y}{1-a} \right) a(1-a)x_1 = x_1(a - y) = x_1 \frac{\delta L(a, y)}{\delta z} \end{aligned}$$

---

---

---

---

---

---

---

---

---

---

These slides are provided by Minhhoai Le, ICSTLab, Phoenicia Ltd.

47

47

1. Shallow Neural Network

Logistic Regression

Code



$$J = 0; dw_1 = 0; dw_2 = 0; db = 0;$$

For i = 1 to m

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J += -[y^{(i)} \log a^{(i)} + (1 - y^{(i)}) \log(1 - a^{(i)})]$$

$$dz^{(i)} = a^{(i)} - y^{(i)}$$

$$dw_1 += x_1^{(i)} dz^{(i)}$$

$$dw_2 += x_2^{(i)} dz^{(i)}$$

$$db += dz^{(i)}$$

$$J /= m; dw_1 /= m; dw_2 /= m; db /= m;$$

Update weights:

$$w_1 := w_1 - \alpha dw_1$$

$$w_2 := w_2 - \alpha dw_2$$

$$b := b - \alpha db$$

---

---

---

---

---

---

---

---

---

---

These slides are provided by Minhhoai Le, ICSTLab, Phoenicia Ltd.

48

48

### 1. Shallow Neural Network

#### Logistic Regression

```
import numpy as np
a = np.array([1,2,3,4])
print(a)

import time
a = np.random.rand(1000000)
b = np.random.rand(1000000)
tic = time.time()
c = np.dot(a,b)
toc = time.time()

print(c)
print("Vectorized version:" + str(1000*(toc-tic) + "ms")
```

#### Code

```
c = 0
tic = time.time()
for i = range(1000000):
    c += a[i]*b[i]
toc = time.time()
print(c)
print("For loop:" + str(1000*(toc-tic) + "ms")
```




---

---

---

---

---

---

---

---

---

---

These slides are provided by Minhhoi Le, ICSTLab, Phenikaa Uin.

49

49

### 1. Shallow Neural Network

#### Logistic Regression

```
dw = np.zeros((nx, 1))
J = 0; dw1 = 0; dw2 = 0; db = 0;
For i = 1 to m
    z(0) = wTx(0) + b
    a(0) = σ(z(0))
    J += - [y(0) log a(0) + (1 - y(0)) log(1 - a(0))]
    dz(0) = a(0) - y(0)
    dw1 += x(0) dz(0)
    dw2 += x(0) dz(0)
    db += dz(0)
J /= m, dw1 /= m, dw2 /= m, db /= m
dw /= m
```

#### Vectorization

One for loop is thus removed!!!




---

---

---

---

---

---

---

---

---

---

These slides are provided by Minhhoi Le, ICSTLab, Phenikaa Uin.

50

50

### 1. Shallow Neural Network

#### Logistic Regression

- $X = [x^{(1)} \ x^{(2)} \ \dots \ x^{(m)}]$
- $Z = [z^{(1)} \ z^{(2)} \ \dots \ z^{(m)}] = w^T X + [b \ b \ \dots \ b] = \text{np.dot}(w, X) + b$
- $A = [a^{(1)} \ a^{(2)} \ \dots \ a^{(m)}] = \text{sigmoid}(Z)$

#### Vectorization




---

---

---

---

---

---

---

---

---

---

These slides are provided by Minhhoi Le, ICSTLab, Phenikaa Uin.

51

51

### 1. Shallow Neural Network

#### Logistic Regression

#### Vectorization



- $dz^{(1)} = a^{(1)} - y^{(1)}$ ,  $dz^{(2)} = a^{(2)} - y^{(2)}$ , ... (all m examples)
- $dZ = [dz^{(1)} \ dz^{(2)} \ \dots \ dz^{(m)}]$
- $A = [a^{(1)} \ \dots \ a^{(m)}]$
- $Y = [y^{(1)} \ \dots \ y^{(m)}]$
- $dZ = A - Y = [a^{(1)} - y^{(1)} \ \dots \ a^{(m)} - y^{(m)}]$
- $db = \frac{1}{m} \sum_{i=1}^m dz^{(i)} = \frac{1}{m} np.sum(dZ)$
- $dw = \frac{1}{m} X dZ^T$

These slides are provided by Minhuy Le, ICSTLab, Phenikaa Utn.

52

52

---

---

---

---

---

---

---

---

---

---

### 1. Shallow Neural Network

#### Logistic Regression

#### Vectorization



```

J = 0; dw = np.zeros((nx,1)); db = 0;
For i = 1 to m
    z(i) = wTx(i) + b
    a(i) = σ(z(i))
    J += - [y(i) log a(i) + (1 - y(i)) log(1 - a(i))]
    dz(i) = a(i) - y(i)
    dw += x(i) * dz(i)
    db += dz(i)
J /= m, dw /= m, db /= m
    
```

```

Z = wTX + b = np.dot(w.T, X) + b
A = sigmoid(Z)
dZ = A - Y
dw = 1/m X dZT
db = 1/m np.sum(dZ)

w := w - α dw
b := b - α db
    
```



These slides are provided by Minhuy Le, ICSTLab, Phenikaa Utn.

53

53

---

---

---

---

---

---

---

---

---

---